

# MEC651

## Instabilities and control of shear flows

### Objectives

The objective of the course is to introduce and adapt modern flow control techniques in order to stabilize flow instabilities and therefore delay transition to turbulence. Both open-loop and closed-loop control strategies will be presented. These issues play a crucial role in both aeronautical and mechanical engineering applications.

Also:

- acquire new methods, algorithms
- numerical practice
- physics involved

### How?

1/3: Theory

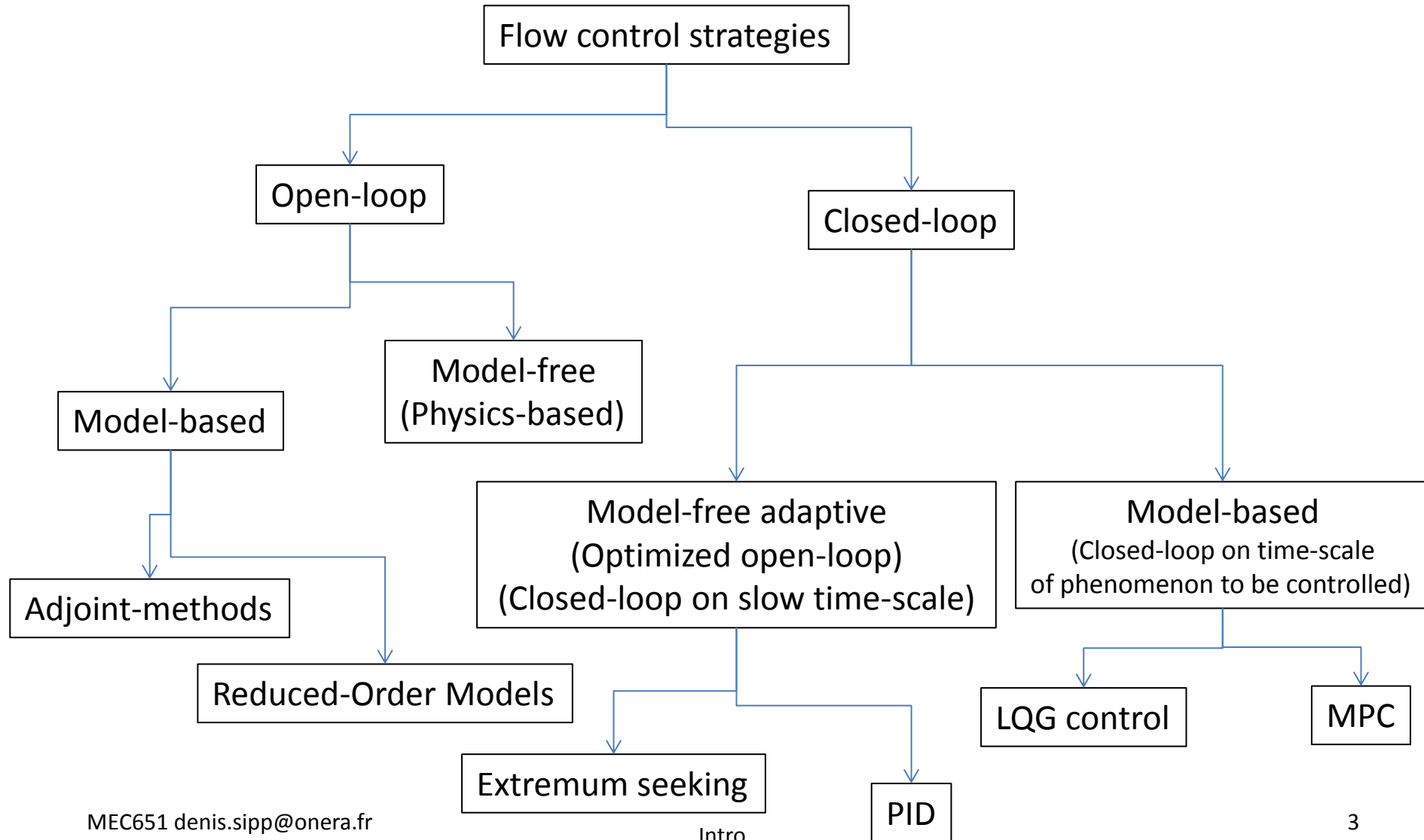
1/3: Mathematical practice

1/3: Numerical practice (codes based on FreeFem++ and Matlab/Octave)

# Motivations

- ❑ Wide range of applications
  - suppression of instabilities
  - exploration of previously inaccessible parameter regimes
  - increase of stability margins
  - diminish sensitivities to external noise sources
  - improve performance (decrease drag)
  - minimize environmental impact
  - Aerodynamics/combustion/aeroacoustics/fluid-structure/...
- ❑ Design of flow control devices for manipulating inherent flow behaviour

# Different types of flow control



# Instabilities

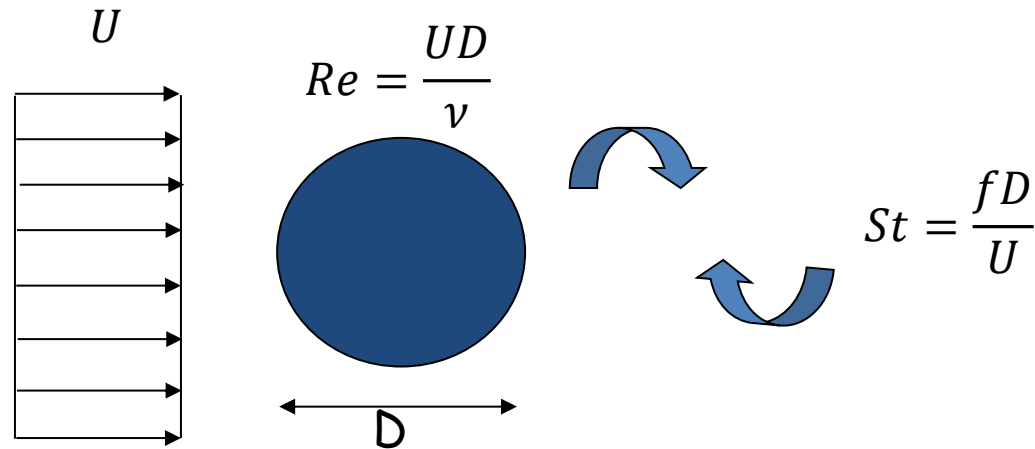
## Oscillator flows

- Frequency spectrum characterized by peaks
- Absolutely unstable flows
- Not sensitive to environmental noise

## Amplifier flows:

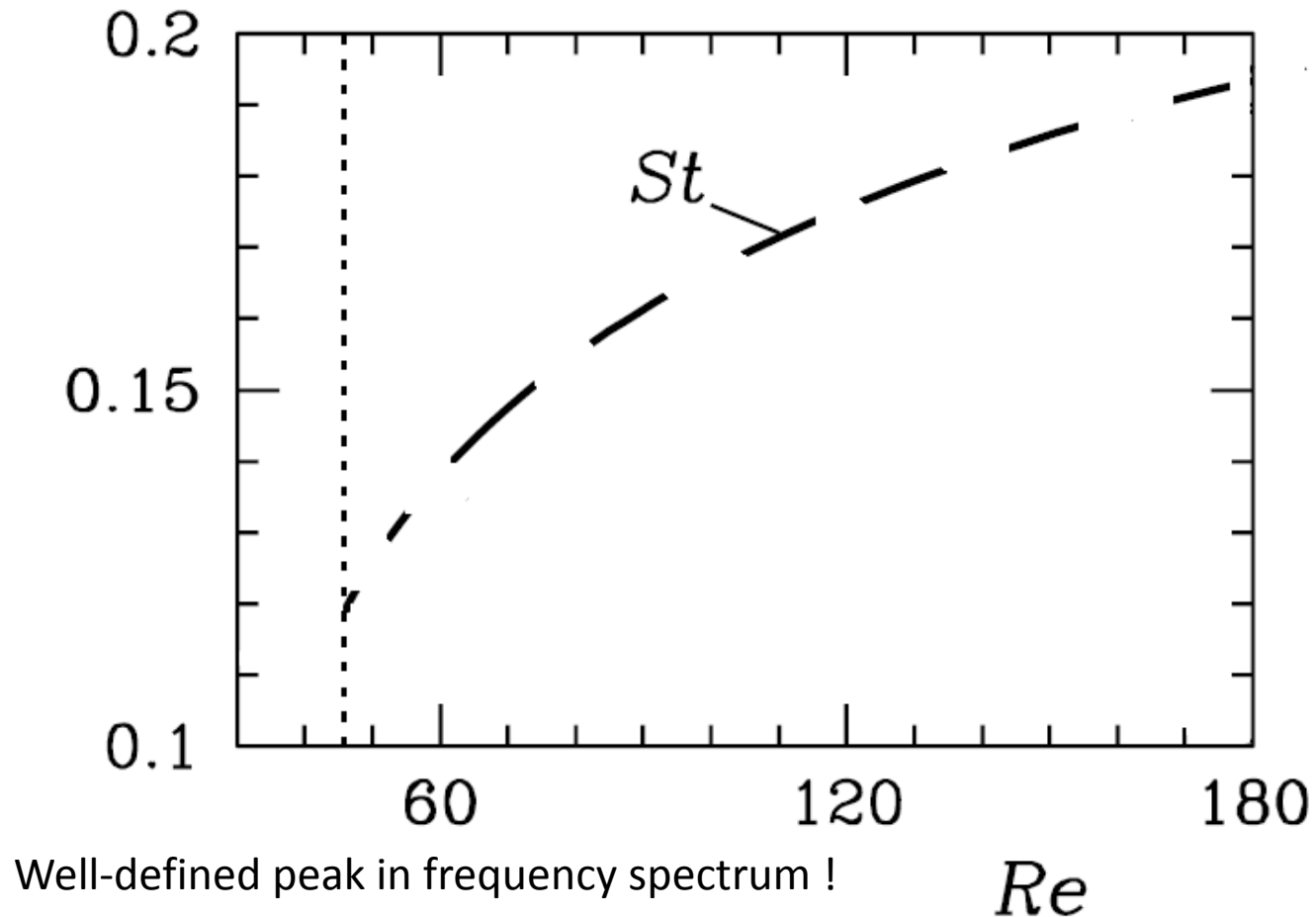
- Broadband spectrum
- Convectively unstable
- Dynamics reflects upstream noise
- Boundary layer flow, jets, shear-layers without counter-flow, wake vortices

# Cylinder flow

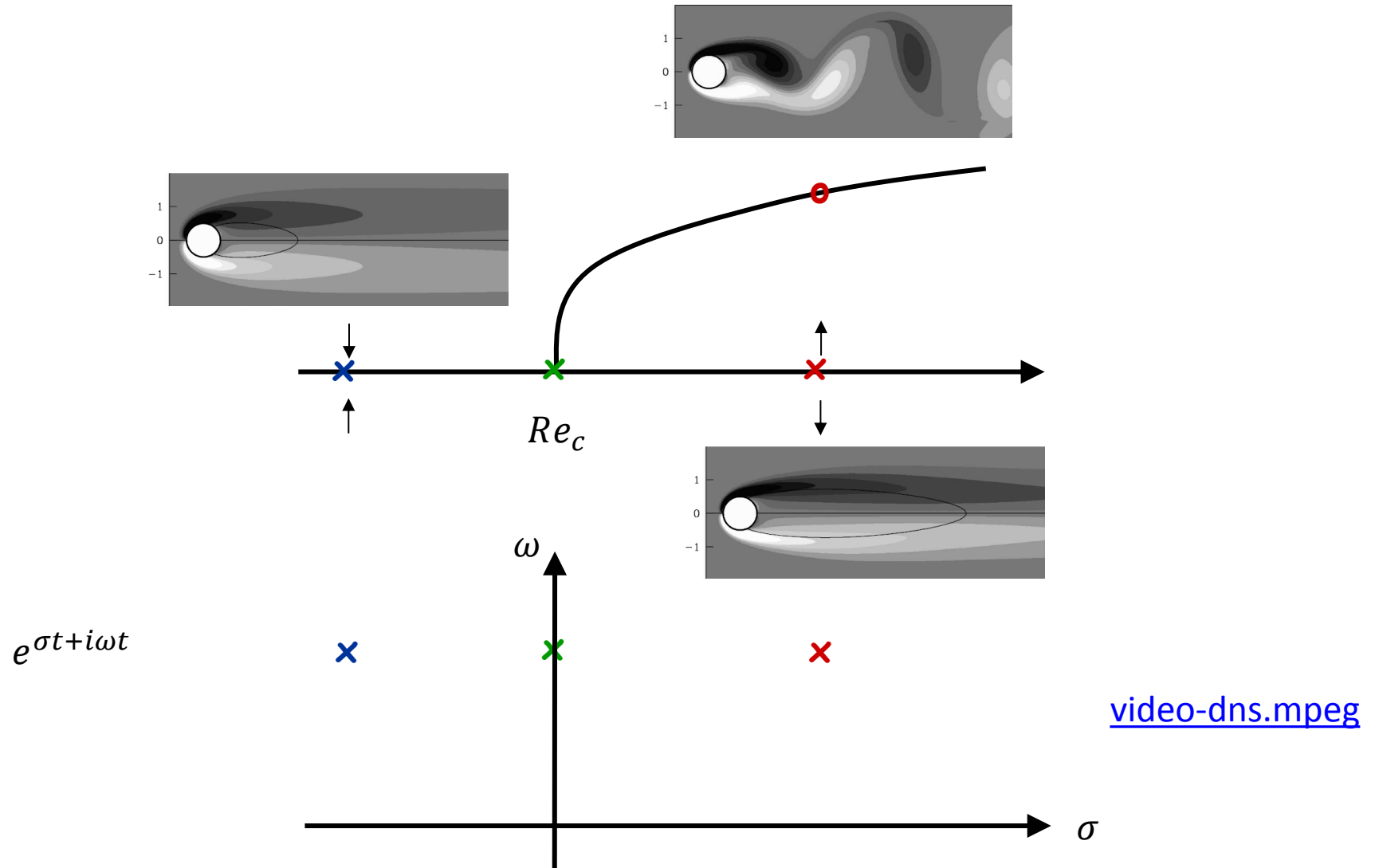


$Re > 47$ : appearance of unsteadiness

# Cylinder flow

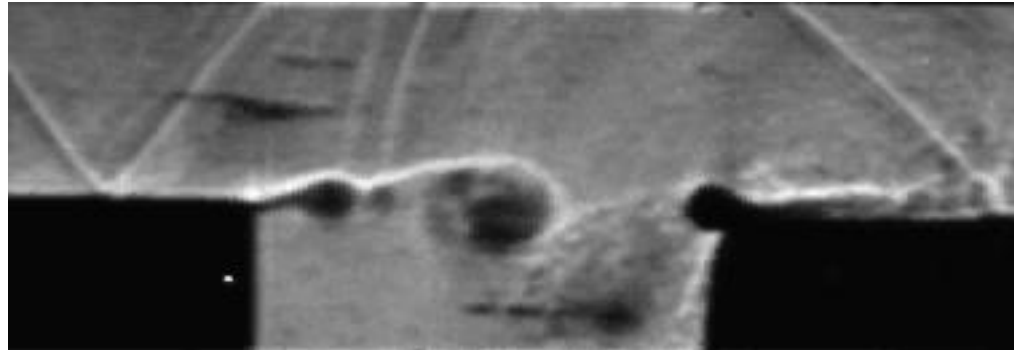


# Oscillator flows / bifurcation

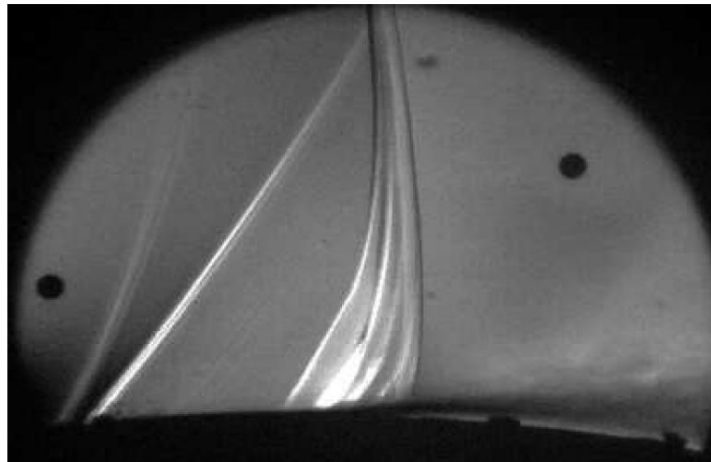


# Other oscillator flows (high Re number flows)

Cavity flow



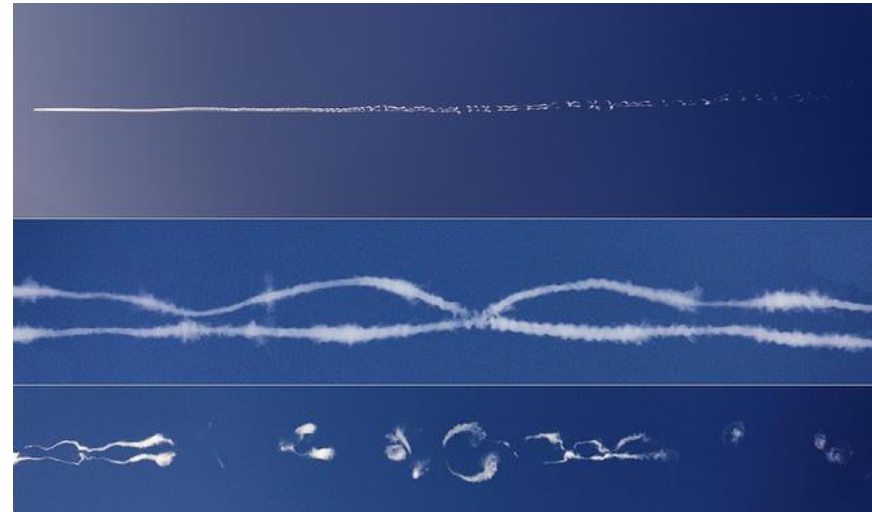
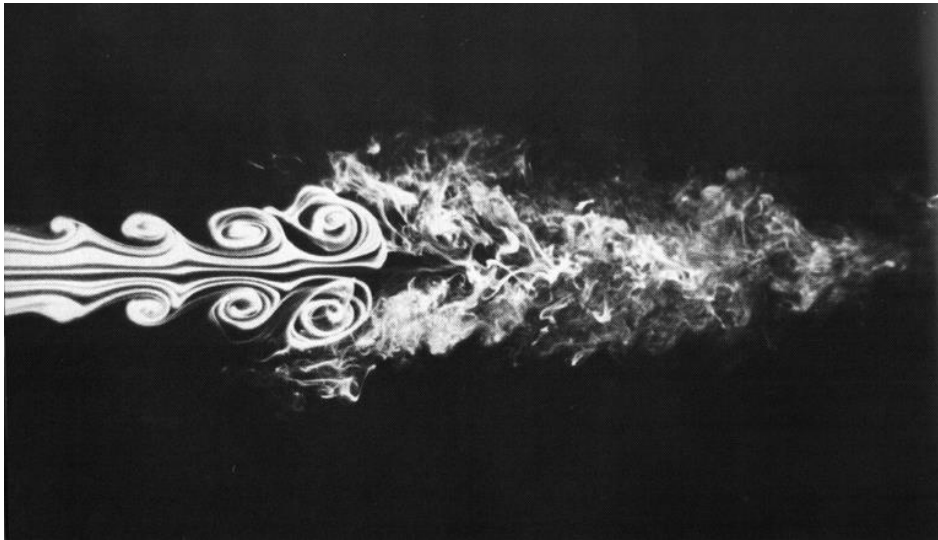
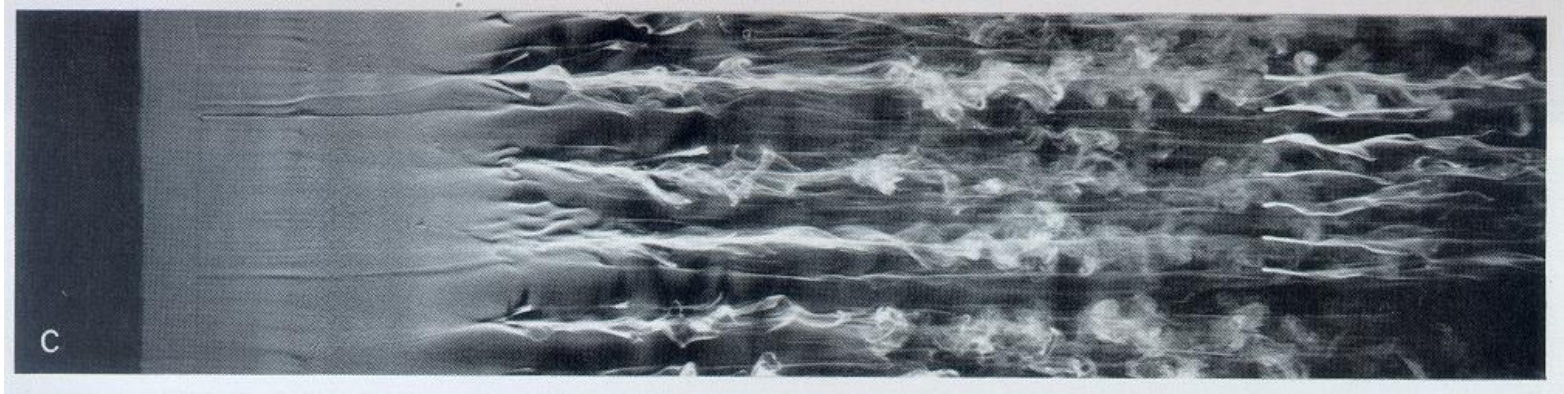
Buffet over aerofoils



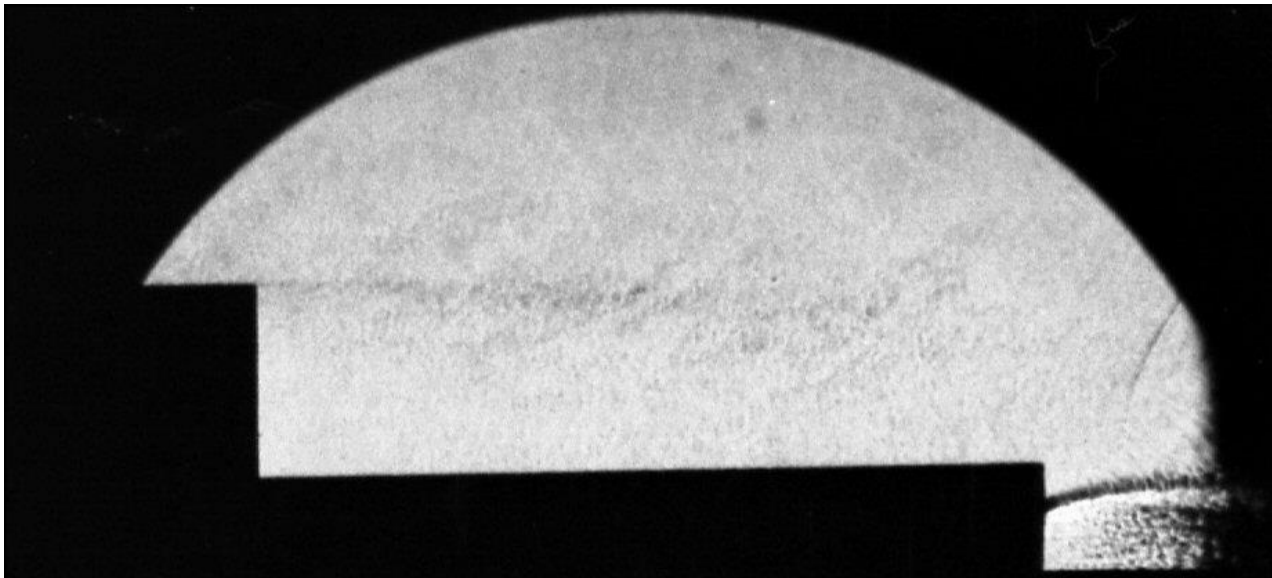
Other : buffet over airfoils, light jets, screeching jets, shear-layers with strong counter-flow



# Amplifier flows

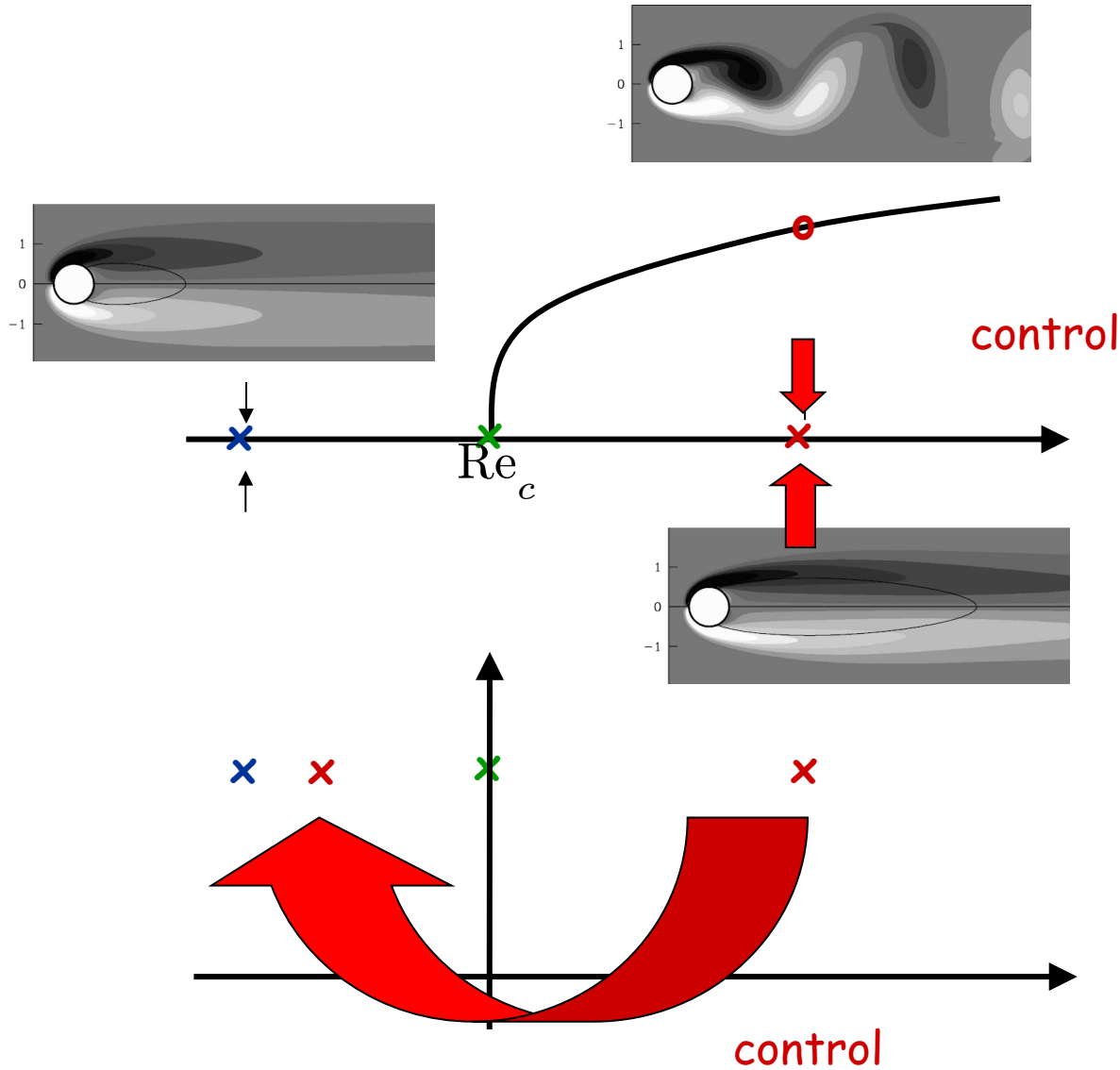


# Oscillator / Amplifier flows

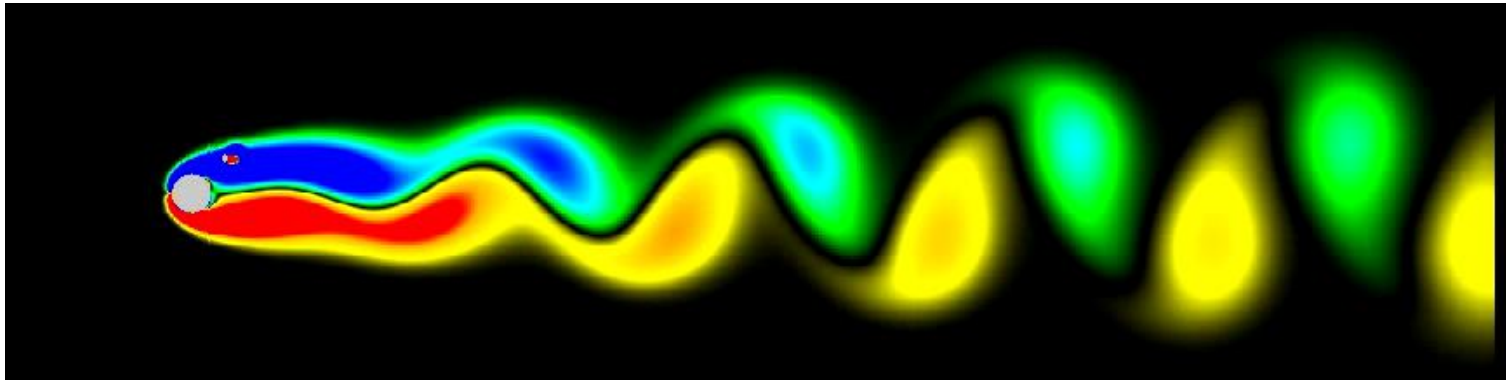
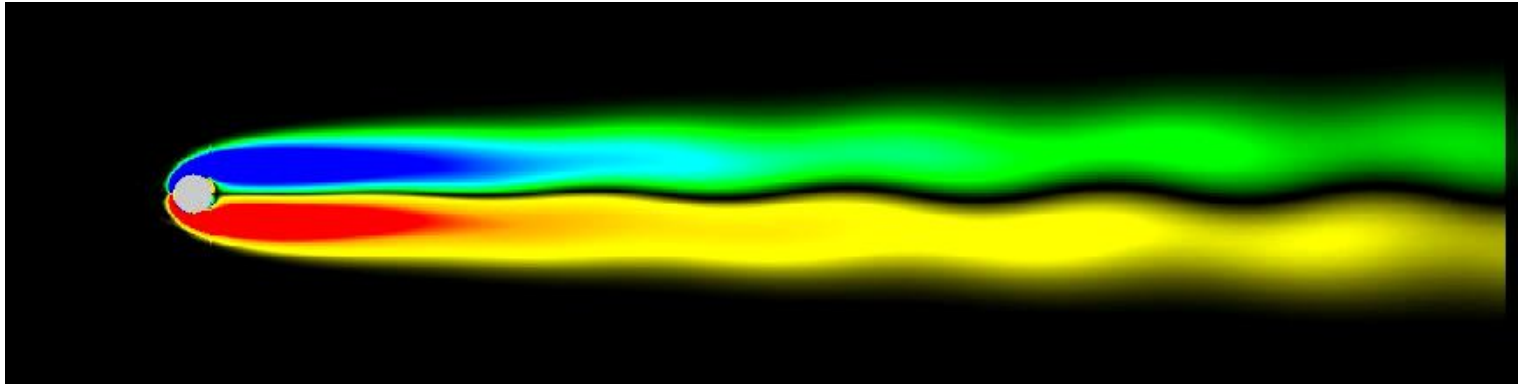


Ariane V after-body, ONERA

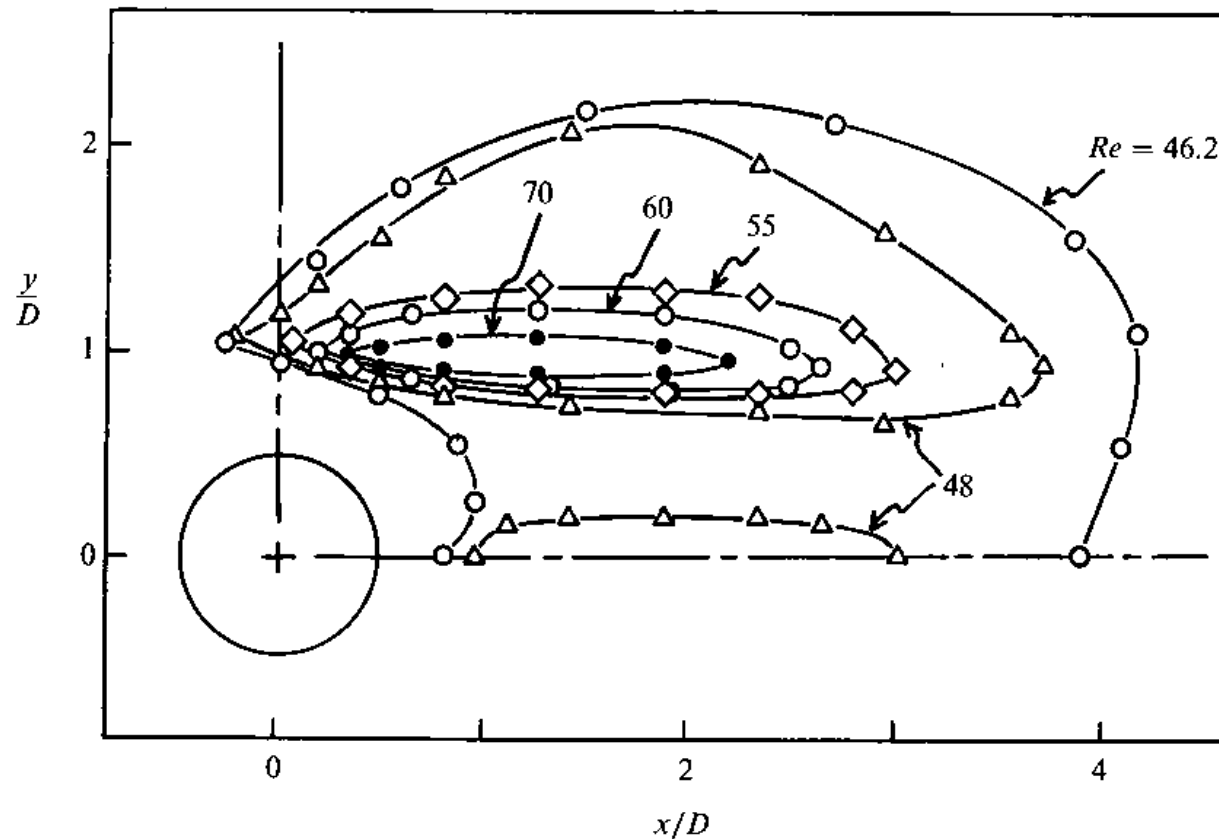
# Control of oscillator flows



# Open-loop control with cylinder

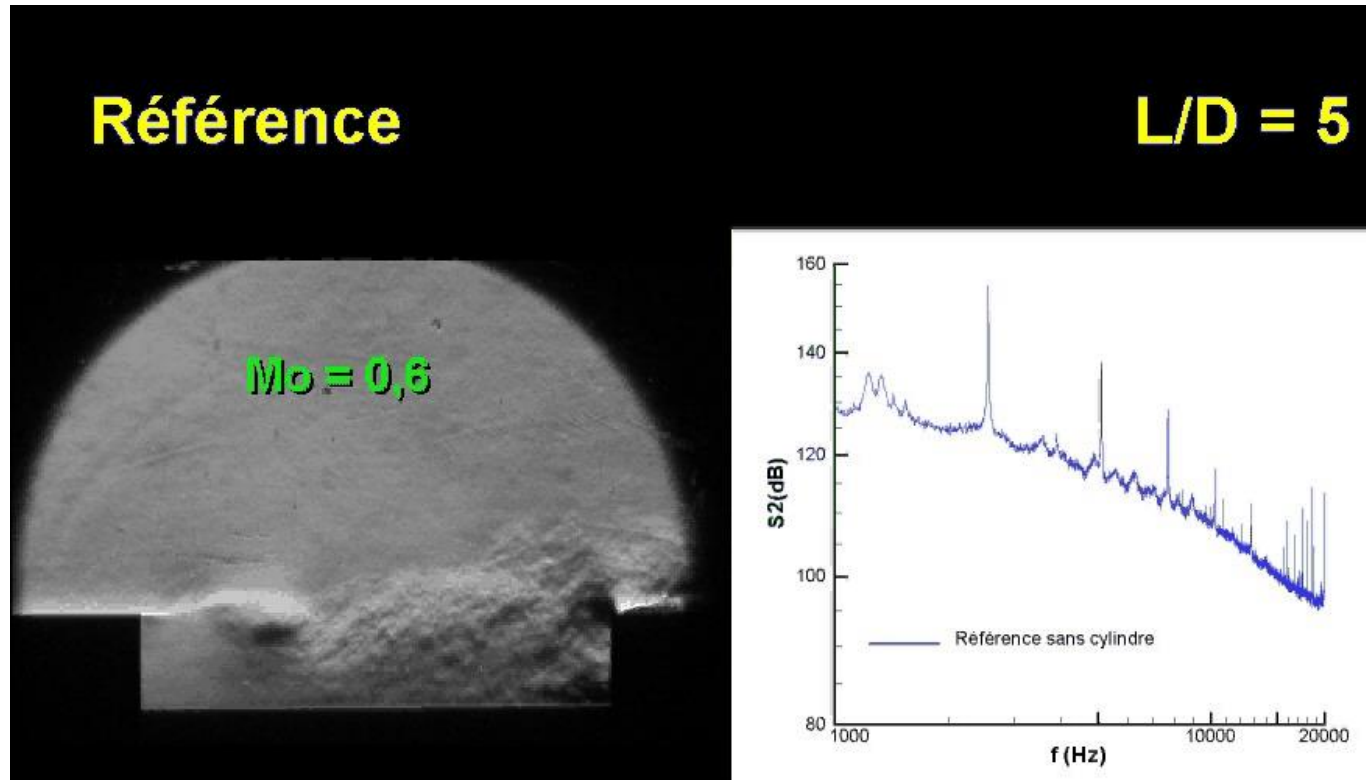


# Open-loop control with cylinder



Strykowski & Sreenivasan JFM 1990

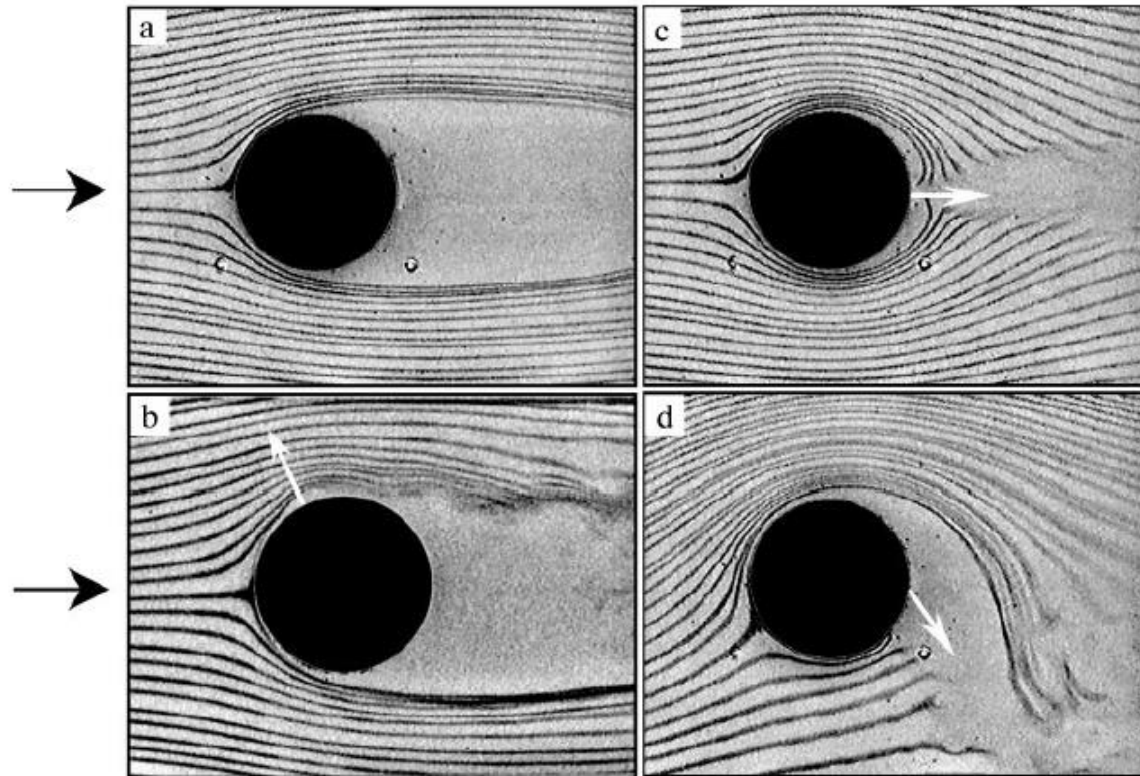
# Open-loop control with cylinder





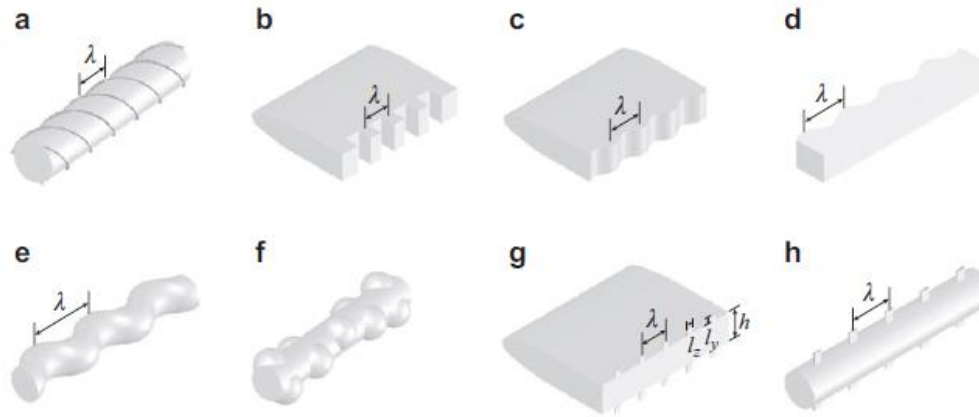
# Open-loop control with symmetry-breaking forcing

Harmonic forcing with synthetic jets



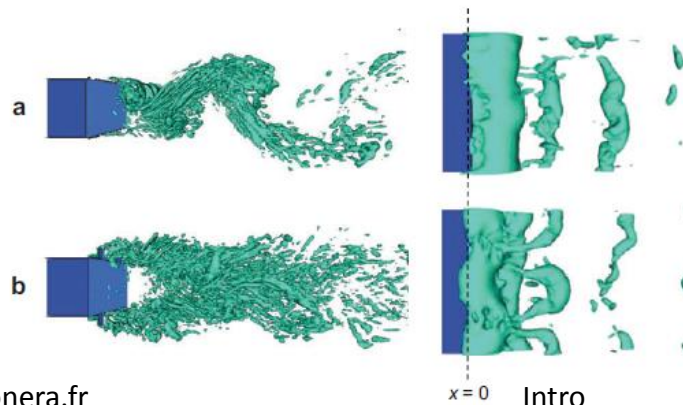
**Figure 7** Smoke of the flow around a circular cylinder visualization: (a) baseline; and (b) actuated:  $\phi = 0$ ,  $\gamma = 60^\circ$  and (c)  $180^\circ$ , and (d)  $\phi = 120^\circ$ ,  $\gamma = 180^\circ$ .

# Open-loop control with symmetry-breaking forcing



**Figure 4**

3D forcing by passive means: (a) helical strake, (b) segmented trailing edge, (c) wavy trailing edge, (d) wavy stagnation face, (e) sinusoidal axis, (f) hemispherical bump, and (g, h) small-size tab.



**Figure 5**

Instantaneous vortical structures in a wake ( $Re = u_\infty b / \nu = 4200$ ): (a) uncontrolled flow and (b) controlled flow with tabs of  $(\lambda/b, l_y/b, l_z/b) = (2, 0.2, 0.2)$ . Shown are the 3D views of vortical structures (left column) and top views of isopressure surfaces (right column). Figure taken from Park et al. 2006.

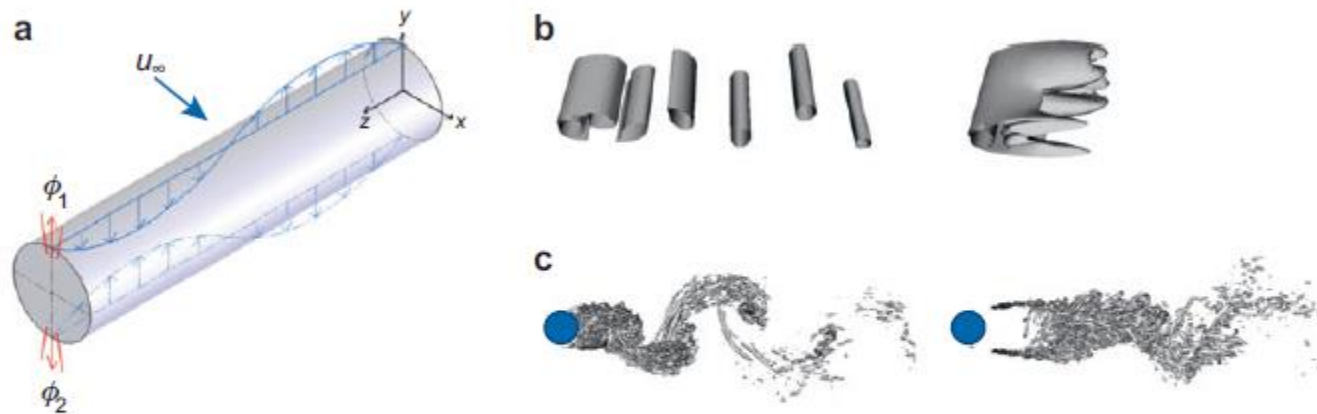
Choi ARFM 2008



# Open-loop control with symmetry-breaking forcing

Wavy spanwise blowing/suction

Choi ARFM 2008



**Figure 6**

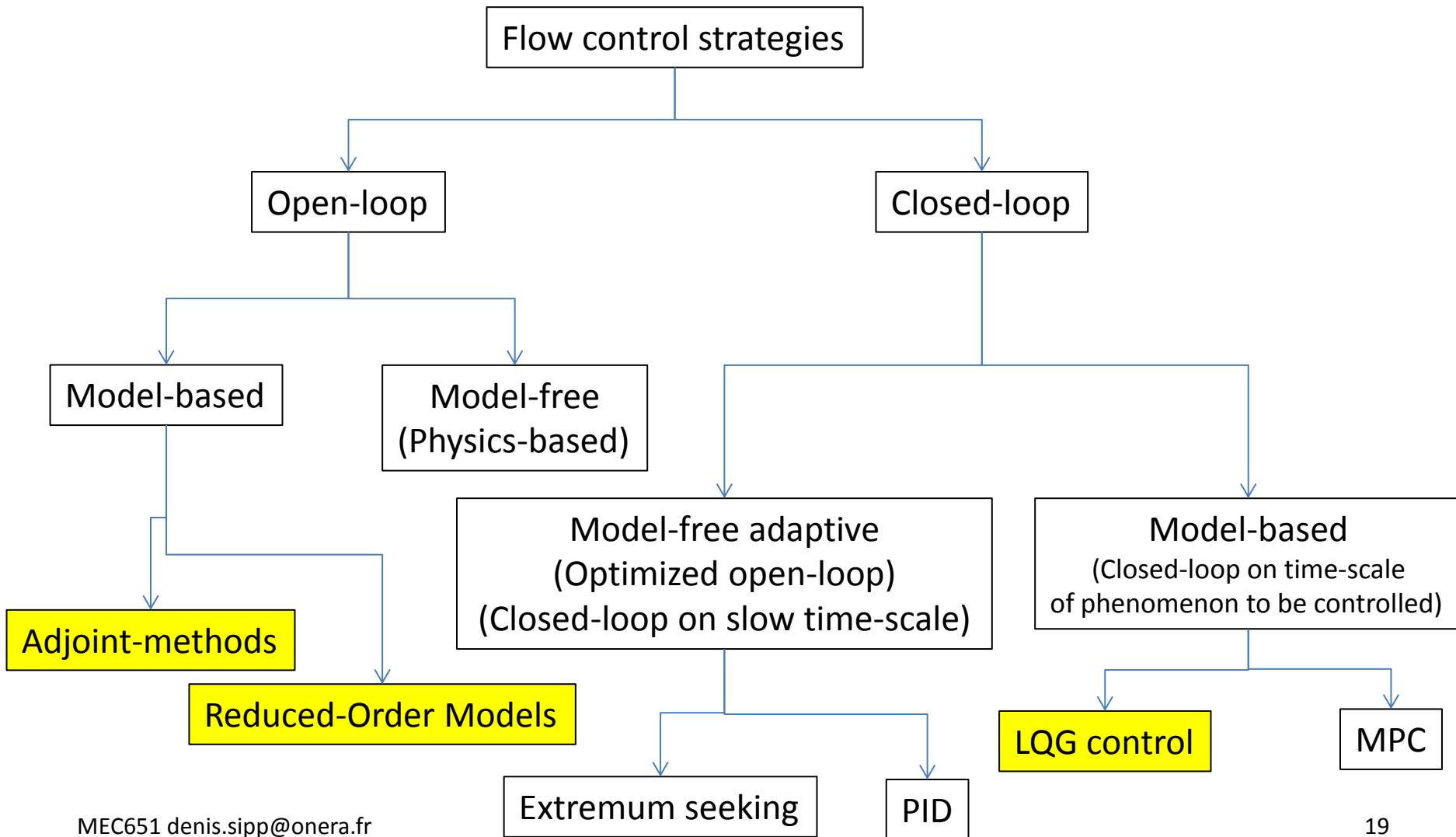
Distributed forcing: (a) schematic of the forcing, (b)  $Re = 100$  ( $\lambda = 5d$ ), and (c)  $Re = 3900$  ( $\lambda = \pi d$ ). Shown in panels b and c are the instantaneous vortical structures without (left column) and with (right column) control. Figure taken from Kim & Choi 2005.

# Model-based closed-loop control with estimator/controller

Estimation problem: [estim.mp4](#)

Control problem: [control.mp4](#)

# Outline of course



# Outline of course

0/ Instabilities and global modes in open shear-flows.

1/ Open-loop control with adjoint methods: variational formulation, adjoint operators, adjoint global modes, eigenvalue sensitivity.

2/ Open-loop control with amplitude equations: the forced Van der Pol oscillator, multiple time-scale analysis, compatibility condition, bifurcation analysis in real systems.

3/ Model reduction with balanced truncation: input/output dynamics, observability and controllability Gramians, Hankel singular-values, balanced basis.

4/ Closed-loop control with estimator / controller setup: Riccati-based feedback control, full-state information control, partial state information control, estimation and Kalman filtering.

All concepts will be illustrated on cylinder and open-cavity flows.